MATHEMATICAL METHODS

Instructor: Ravi Venkatramani
Office: B125
Email: ravi.venkatramani@tifr.res.in
Phone: 2278 2064 (off), 9503233302 (cell)

Course start date: August 13th(Thursday)
Hours: 9:30 am – 11:30 am
Days: Tuesdays and Thursdays
Office Hours: 11 am – 1pm
(Mon Wed Fri)

Syllabus

1. **Complex numbers and analysis (6 Lectures)**
    a. Argand`s diagram, complex algebra
    b. de Moivre`s theorem and applications
    c. Functions of complex variables
        i. Analytic functions, multi-valued functions, singularities and zeros
        ii. Complex integration and series expansions
        iii. Residue theorem and applications, Contour integration

2. **Vectors, Vector spaces and Matrices (7 Lectures)**
    a. Vectors
        i. Vector algebra, differentiation and integration
        ii. Vector operators, gradient, divergence, curl
        iii. Line, surface, and volume integrals
        iv. Integral (Green`s, Divergence, and Stokes) theorems and applications
    b. Matrix representations and operators
        i. Notation, algebra and matrix operations, Special square matrices
        ii. Change of basis, eigenvalues and eigenvectors
        iii. Applications

3. **Orthogonal functions and Integral Transforms (10 Lectures)**
    a. Orthogonal functions
        i. Even, odd, orthogonal, and orthonormal functions
        ii. Fourier series, expansion in terms of orthonormal functions
        iii. Gram-Schmidt orthogonalization, Schwarz inequality
        iv. Hermite, Legendre, and Laguerre polynomials and associate properties
    b. Fourier transforms
        i. Definitions, Properties
        ii. convolutions/deconvolutions
        iii. Correlations functions, energy spectra
        iv. Parseval`s theorem
    c. Laplace transforms
        i. Definitions and properties
        ii. Transforms of derivatives and integrals

4. **Differential Equations (13 Lectures)**
    a. Ordinary differential equations (ODE) and elementary methods
        i. Classifications of equations, exact, inexact, linear, nolinear, homogenous, nonhomogenous.

ii. Direct integration, separation of variables, integrating factors

b. Higher order ODE and solutions
   i. Linear equations with const coefficients,
   ii. Linear equations with variable coefficients,
   iii. Solutions using Laplace transforms
   iv. Solutions using Greens functions
c. Series solutions of ODE
   i. Solutions about ordinary and singular points
   ii. Wronskian and derivative methods
   iii. Fuch`s theorem
d. Eigenfunction methods
   i. Operators:Adjoint, Hermitian and properties
   ii. Sturm-Liouville equations
   iii. Superposition of eigenfunctions
e. Partial differential equations
   i. Diffusion, Wave, Laplace, Poisson, and Schrodinger equations

Text/Reference Books:

1. K. F. Riley, M. P. Hobson, S.J. Bence, *Mathematical methods for physics and gineering*,3rd edition, Cambridge University Press (2002).
2. M. L. Boas, *Mathematical methods in physical sciences*, 3rd editions, Wiley-India(2006)
3. J. M. Anderson, *Mathematics for quantum chemistry*, Dover Publications (2005)
4. W. W. Bell, *Special functions for Scientists and Engineers*, Dover Publications (1996)

Grading:

Two exams with equal weight: Part-I in October and Part-II in December
Assignments every two weeks + in-class discussion
Grade distribution (50% for each part)**:**
Assignments (10%) + in-class discussion (6 presentation + 4 (participation)=10%) + written exam (30%)